

Fountains

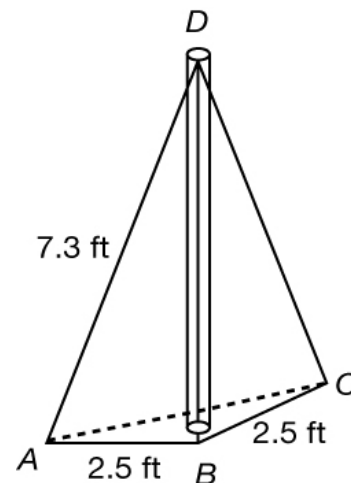
Fountain designs often incorporate geometric elements. These elements provide balance and beauty for the beholder.

1. This diagram shows a fountain rising through a pyramid in which \overline{DB} is perpendicular to the plane containing points A , B , and C .

a. Explain how you know that $\triangle ADB$ and $\triangle CDB$ are congruent.

b. Find CD . Justify your reasoning.

c. What type of triangle is $\triangle ABC$? Justify your response.

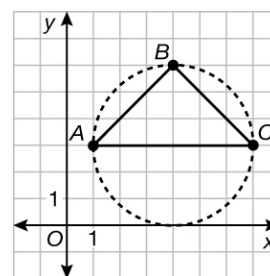


2. This diagram shows three points A , B , and C on a circle. A fountain is to be located at the point where the perpendicular bisectors of \overline{AC} , \overline{BC} and \overline{AB} intersect.

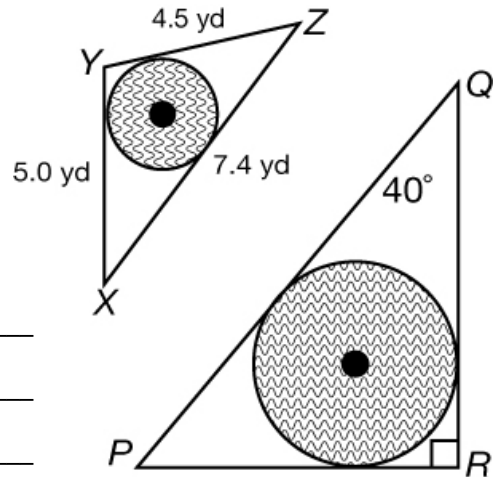
a. Find an equation for the perpendicular bisector of \overline{AC} . Explain your reasoning.

b. Find an equation for the perpendicular bisector of \overline{AB} . Show your work.

c. Find the coordinates of the point where the perpendicular bisectors of \overline{AB} and \overline{AC} intersect. Show your work.

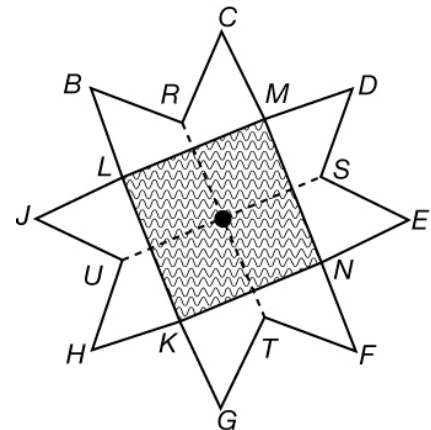


3. There are two memorial fountains in the centers of two circles each nesting snugly inside the triangular parks shown here.
- List the three angle measures and three sides in $\triangle PQR$ in order from least measure to greatest measure. Justify your reasoning.



- List the three angle measures of $\triangle XYZ$ in order from least to greatest. Justify your reasoning.

4. This diagram shows an eight-point star with a fountain centered in square $KLMN$. In the diagram $LM = 4.8$, $BL = 3.0$, and each dashed line segment is 1.0 units long.



- Find the area of polygon $LBRCM$. Justify your reasoning.

- Find the total area of the eight-point star.

5. This diagram shows $\triangle MNY$. A fountain is to be built where the angle bisector of $\angle M$ intersects \overline{NY} , point X . How do $\triangle MXY$ and $\triangle MXN$ compare? Use the diagram to explain your response.

